

# Lorentz Motor With Stationary Magnets and Coils Applied in a 6-DOF Contactless Motion Stage

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## Abstract

This paper presents a novel electro-magnetic motor principle that has all the advantages of Lorentz-type actuators and but works with stationary permanent magnets and stationary coils. Different candidate motor solutions will be discussed and the most attractive solution is selected.

This novel motor principle has been incorporated into a 6-degree-of-freedom (6DoF) Planar Active Magnetic Bearing (PAMB) design. The dimensioning of this motor type to the required specifications for this application is presented. Results of experiments on a modified existing setup show that the motor operates according to the presented theory. The results of our work indicate that future systems can benefit from more modular designs which take symmetry considerations into account. A sketch of the potential future configuration is given.

## 1 Introduction

In the design of stages that must move in a horizontal plane with relatively large XY-movement disturbing forces from traditional bearings will limit the final accuracy. The use of Active Magnetic Bearings (AMBs) enables to virtually eliminate these disturbances. The generation of driving forces generally introduces heat dissipation, which gives a potential loss of accuracy.

The creation of combined electro-magnetic suspension and propulsion systems has been a focus in our research at the Delft University of Technology. F. Auer designed a modular 6DoF table, consisting of 3 contactless Suspension and Propulsion Units (SPU) [1]. Leveraging of Auer's work A. Molenaar designed a Planar Active Magnetic Bearing (PAMB) [3], which integrates a reluctance type suspension and a Lorentz-type propulsion with moving coils (moving armature). Permanent Magnets (PMS) are used to generate the bias flux.

Disturbing forces introduced by the feeding wires of the propulsion coils and heat generation by the coils on the rotor form a potential limitation for the performance of the PAMB. This article presents a novel electro-magnetic propulsion principle which deals with these limitations, while keeping the advantages of Lorentz-type actuators.

## 2 Macroscopic Force Equation

This section will introduce the underlying theory to explain the forces that act in a system consisting of a coil, a PM, and a yoke. By applying the virtual work method the total summed magnetic force  $F_m$  on a yoke part movable in the  $x$  direction can be derived (see [4, p.190] and [2, p.55]):

$$F_m = I \frac{d\Phi_{cm}}{dx} \Big|_{(I=0)} + \frac{1}{2} I^2 \frac{dL_c}{dx} - \frac{dW_m(x)}{dx} \Big|_{(I=0)}, \quad (1)$$

with  $I$  the current through the coil,  $\Phi_{cm}$  the flux enclosed by the coil and originating from the PM,  $x$  the position of the yoke,  $W_m$  the magnetic field energy for  $I = 0$  (i.e. from the PMS), and  $L_c$  the self-inductance of the coil. The first term is the force due to mutual flux linking, which varies with the flux from the PMS enclosed by the coil and is called *mutual force*. In most applications the magnetic induction ( $B$ -field) generated by the coil can be neglected, and the mutual force can be calculated  $F = BIl$ , the well-known *Bil-law* for Lorentz forces ([2]).

The second term is a function of  $I^2$  and therefore independent of the direction of the current flow. This term always acts to increase the inductance ( $\frac{dL_c}{dx} > 0$ ) or to decrease the magnetic reluctance and is therefore called *reluctance force*.

The third term represents the force due to a change in energy from the permanent magnet  $W_m$ , which is also a *reluctance force*.

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### 3 Wireless Propulsion: Moving Iron

A Lorentz force originates from the moving charges in a wire 'I'. Thus, a Newtonian reaction force must act on the source of the magnetic flux density ( $B$ ). A novel drive concept<sup>2</sup>, referred to as *moving iron*, makes use of this reaction force. A rotor bar is driven by Lorentz forces without coils or magnets on it.

#### 3.1 Working Principle

To understand the working principle of moving iron, consider a simple case as depicted in Figure 1. The I-shaped rotor is assumed to be supported on bearings that restrict movement to horizontal displacement<sup>3</sup>. Furthermore, the ferromagnetic C-shaped stator yoke is considered an ideal flux guidance ( $\mu_r = \infty$ ). Therefore, the stator part between permanent magnet and air gap can be elongated without effect, which is indicated by the parallel line pair. Because the magnet poles travel through the flux guidances towards the crossing of the bars that define the air gap, the flux lines leave the stator at a position that moves along with the rotor iron. Thus the rotor behaves as a virtual source of  $B$ -field(!), while the actual PM can be positioned at a fixed position of the stator circuit. As a result, the reaction force of the Lorentz force act on the rotor.

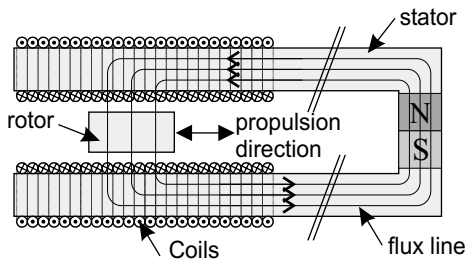


Figure 1: Winding scheme for a moving iron driven rotor, with a spiral wrapped coil option.

Since the guiding flux bars are assumed to be ideal and the air gap height to be constant, the magnetic field energy term resulting from the PMS  $W_m$  in (1), does not change with a horizontal change of position. For the same reason the self inductance of the coil will not change. The term  $\frac{\Phi_{cm}}{dx}$  is non-zero and does

<sup>2</sup>This concept is described in [4], but was not presented before.

<sup>3</sup>The suspension of the rotor is not discussed here, see [3, 4]

not change with the position  $x$  because of the equally divided copper. Thus a mutual (Lorentz) force is generated with  $F \propto I$ . A qualitative check is to verify if the enclosed flux of the winding changes while displacing the rotor.

To understand better the difference in a classical approach and the moving iron principle consider Figure 2.

#### Option A, C and D do not propel the rotor

With option A shown in Figure 2, the enclosed flux will increase only with rotation. Hence only a bending moment on the rotor occurs. Option C (fixed to the rotor) will not work either because the enclosed flux is invariant with position change. The same holds for option D (alternatively, the Lorentz forces at both sides of the current loop will counter-balance each other).

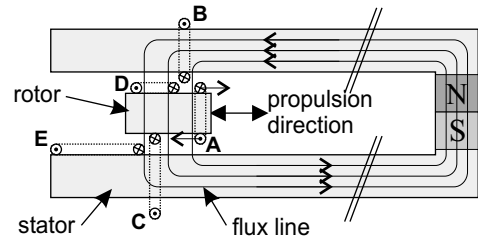


Figure 2: Sketch of a simple linear drive showing five optional drive schemes of which some will lead to a moving iron propulsion.

#### Option B, and E do propel

To get a nett variation of the enclosed flux with a displacement, the return path of the current needs to be positioned outside the air gap region, which is the case with options B and E.

### 3.2 Moving Iron Winding Schemes

Moving iron requires a yoke configuration where the field moves with the rotor while the field source itself (a permanent magnet or a field coil) is fixed at a remote position of the stator. This is the case in the setup shown in Figure 3, where five more practical moving iron winding schemes are depicted. Options 1 and 2 are flat coils that are wound concentric and with a blending displacement, respectively. These will deliver the same force as the winding option depicted in Figure 1 but with about 50% less power dissipation.

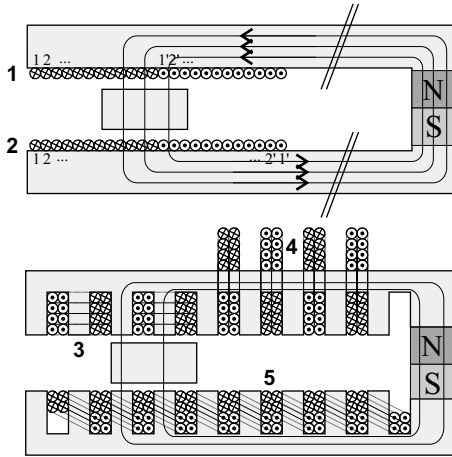


Figure 3: Alternative winding schemes for a moving iron driven rotor. Top: two flat wound coil schemes. Bottom: three buried coil options on salient poles.

With options 3, 4 and 5 more ampère-turns can be coupled to the permanent magnet flux for a given motor length. However, parasitic reluctance forces will occur, called cogging. Option 5 has overlapping coils, which is beneficial for smooth and efficient commutation.

### 3.3 Advantages

Active magnetic bearings utilizing the moving iron principle show three major advantages. First, the positioning accuracy of a moving iron setup is not limited by disturbing forces introduced by the feeding wires of the rotor coils. Secondly, the heat dissipated by the coils can be carried away through the stator material by conduction. Finally, a light weighted and compact linear driven rotor with planar freedom can be created that is not influenced by the size of the coils or the size of the permanent magnets used.

## 4 Towards a Prototype

### 4.1 Practical Implementation

The novel moving iron principle can be implemented by modifying the PAMB set-up of Molenaar described in [3, 4]. The less complex moving iron winding scheme of Figure 1, was applied because of practical reasons, although this is not the most power efficient winding scheme. This is shown in Figure 4. Each

pair of upper and lower propulsion coils is series connected, thus assuring symmetrical loading.

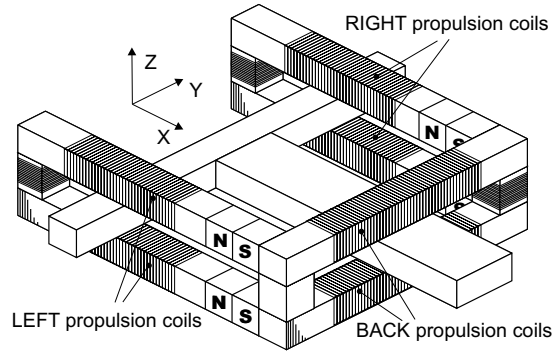


Figure 4: Planar active magnetic bearing with moving iron propulsion.

### 4.2 Dimensioning of the Coils

Next the dimensioning of the coils in Figure 4 is discussed. The size of the flux guiding bars and the rotor (upper part of the T) is  $20 \times 20 \text{ mm}^2$ . The total air gap between the rotor and stator is 1.1 mm. An aim in the design of the PAMB is to have an acceleration of  $1g$ . With a rotor mass of 3.5 kg, a force of 34.4 N is needed. Forces in the  $x$ -direction are generated by the left and right propulsion coils in a total of four air gaps. Assuming a  $B$ -field in the air gaps of 1 T, we can calculate with the *Bil-law* that the Ampère turns needed in one airgap is 429. This must be equal to the cross section area of the airgap ( $1 \times 20 \text{ mm}^2$ ) times the filling factor times the maximum current density ( $\rho_{i,\max}$ ). Taking  $\rho_{i,\max}$  equal to  $33 \text{ A/mm}^2$ , the gap filling factor that is needed is 65%.

The maximum peak current that amplifier used in the setup can deliver is 4 A, which determines the minimum wire diameter to 0.39 mm. This means that we need two or three layers.

To allow to probe the flux density in the test setup the stator is wound with one layer of a wire with 0.55 mm core and .58 mm outer diameter. This reduces the filling factor to 41% and  $\rho_{i,\max}$  to  $16.8 \text{ A/mm}^2$ . The  $B$ -field realized in the test setup is 0.6 T. This results in a propulsion force of  $F = 0.6 \cdot 1 \cdot 20 \cdot 0.41 \cdot 16.8 \cdot 20 \cdot 10^{-3} = 1.65 \text{ N}$  per air gap. Thus the total force is  $4 \cdot 1.65 = 6.6 \text{ N}$  and the maximum acceleration  $1.9 \text{ m/s}^2$ .

### 4.3 Experimental Results

The iron moving principle was applied to the PAMB test set-up as described in [3, 4]. The obtained relevant results are given in the table below.

Table 1: Experimental results of the PAMB with the moving iron principle applied.

characteristic	Aim	Realized
square planar range [mm]	100	130
suspended mass [kg]	3	3.37
position stability $\pm 2\sigma$ [nm]	50	75
air gap height (clearance) [mm]	- (0.1)	1.1 (0.4)
magnetic induction [T]	1	0.6
propulsion force [N]	-	6.5
acceleration [m/s <sup>2</sup> ]	9.81	1.9

Comparing the propulsion force calculated by the *Bil-law* of 6.6 N, with the realized propulsion force of 6.5 N, confirms that the propulsion force in the moving iron principle may be calculated using the *Bil-law*.

### 5 Future Research

The *moving iron* principle was successfully applied in the PAMB. However magnetic cross-coupling between the three bearing positions, the asymmetric layout of the PAMB setup and the non-modularity prevents ultimate performance in positioning. Therefore a new design is suggested.

A modular design that utilizes the moving iron principle will allow further improvement of positioning accuracy. Figure 5 shows an example setup of three identical motor-bearing modules. Each module independently suspends and propels one leg of a three legged rotor in 2DoF, thus obtaining a 6DoF PAMB. The propulsion force is exerted at the center of gravity in any planar position, while there is no magnetic coupling between the three bearing positions.

No wires are attached to the rotor. Each motor-bearing module consists of a U shaped stator circuit. The working principle of the this stator circuit is similar to the working principle of the PAMB, taking into account only the left and the bottom part of the stator circuit shown in Figure 4 and "bending" these towards each other. As Figure 5 shows a concept rather than a fixed setup, its layout can easily be adapted to fulfill the needs of future applications.

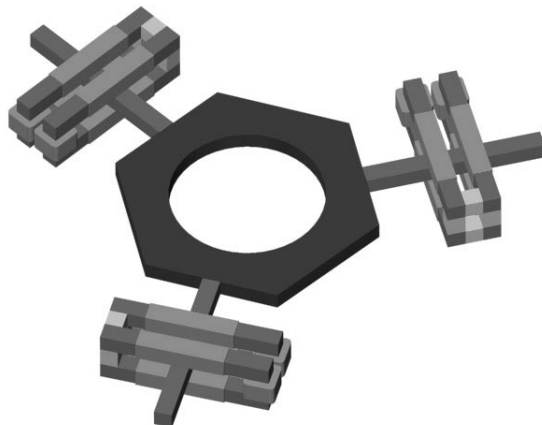


Figure 5: An example setup for a 6DoF PAMB with moving iron propulsion.

### 6 Conclusions

A novel electro-magnetic motor principle has been designed and incorporated into a planar magnetic bearing system. The principle has all the properties of Lorentz-type actuators, while having stationary coils and magnets. The motor principle has been tested and fulfills our expectations. Finally, a sketch of a novel motor-bearing design has been presented, utilizing the motor principle described. This modular and symmetrical setup seems very promising for applications where ultra precise positioning and thermal management is of concern.

### References

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